

Let $f(x) = 5x^2$ and $g(x) = 3x^2$. Perform the indicated operation and state the domain.

1. $f(x) + g(x)$

$$5x^2 + 3x^2$$

$$8x^2$$

D: all Real #'s

2. $f(x) - g(x)$

$$5x^2 - 3x^2$$

$$2x^2$$

D: All real #'s

3. $f(x) \cdot g(x)$

$$(5x^2)(3x^2)$$

$$15x^4$$

D: All real #'s

4. $\frac{f(x)}{g(x)}$

$$\frac{5x^2}{3x^2} = \frac{5}{3}$$

D: All real, $x \neq 0$

5. $f(g(x))$

$$5(3x^2)^2$$

$$5(9x^4)$$

$$45x^4$$

D: All real #'s

5. $g(f(x))$

$$3(5x^2)^2$$

$$3(25x^4)$$

$$75x^4$$

D: All real #'s

Verify that f and g are inverse functions.

7. $f(x) = x - 7$; $g(x) = x + 7$

$$f(g(x)) = (x+7) - 7$$

$$= x$$

$$g(f(x)) = (x-7) + 7$$

$$= x$$

8. $f(x) = 6x^3$; $g(x) = \sqrt[3]{\frac{x}{6}}$

$$f(g(x)) = 6 \left(\sqrt[3]{\frac{x}{6}} \right)^3$$

$$= 6 \left(\frac{x}{6} \right) = x$$

$$g(f(x)) = \sqrt[3]{\frac{6x^3}{6}} = \sqrt[3]{x^3} = x$$

Find the inverse of the function.

9. $f(x) = 3x + 10$

$$y = 3x + 10$$

$$x = 3y + 10$$

$$x - 10 = 3y$$

$$\frac{x - 10}{3} = y$$

10. $f(x) = -\frac{3}{8}x^7$

$$y = -\frac{3}{8}x^7$$

$$x = -\frac{3}{8}y^7$$

$$-\frac{8}{3}x = y^7$$

$$\sqrt[7]{-\frac{8}{3}x} = y$$

11. $f(x) = x^2 - 9, x \geq -9$

$$y = x^2 - 9$$

$$x = y^2 - 9$$

$$x + 9 = y^2$$

$$\sqrt{x + 9} = y$$

12. The cost (in dollars) of g gallons of gasoline can be modeled by $C(g) = 3.15g$. The amount of gasoline used by an SUV can be modeled by $g(d) = 0.025d^{1.24}$ where d is the distance (in miles). Find $C(g(d))$. Evaluate $C(g(500))$. What does $C(g(500))$ represent?

$$\begin{aligned} * C(g(d)) &= 3.15 (0.025d^{1.24}) \\ &= 0.07875d^{1.24} \end{aligned}$$

$$\begin{aligned} * C(g(500)) &= 0.07875 (500)^{1.24} \\ &= 0.07875 (2221.89) \\ &= \$174.97 \end{aligned}$$

* $C(g(500))$ Represents the cost to travel 500 miles.